

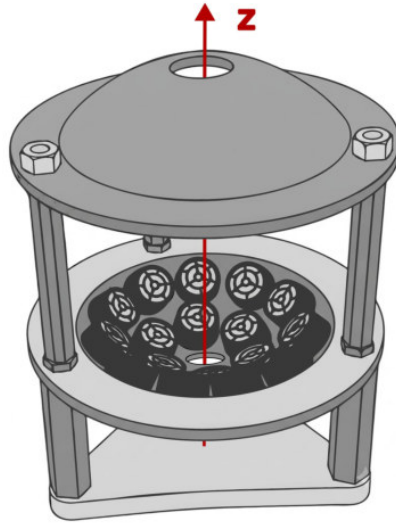
Acoustic levitation (20 pts)

An acoustic levitator consists of transducers which convert an electrical signal into intense sound waves. The acoustic pressure of the resulting interference pattern can levitate small objects close to the nodes of the pattern.

Warning: Avoid short-circuiting the connections on the top and bottom of the levitator.

The tasks E1-E7 of this exam are designed to be independent of each other's results. You may skip tasks you are struggling with.

For the following tasks, consider only the nodes on the z-axis. For task E3 and onward, use only the centremost node. The Mode X switch on the electrical box (F), see Fig. 1, should be in position O.



Task E1: Probing the acoustic field (1.0 pts)

To get familiar with the acoustic field, use the green LEDs (A) and the transducer (B) to construct a tool that emits light according to the local acoustic intensity. A transducer is a capacitor whose charge depends on the mechanical pressure applied to it.

- Draw a circuit diagram for your tool. (0.5 pts)
- Use your tool to roughly estimate the distance between two adjacent antinodes on the z axis in the centre of the levitator. (0.5 pts)

Task E2: Acoustic levitator properties (4.0 pts)

In what follows, to levitate a small solid object, the voltage of the connected power supply can be initially put to a high voltage, for example 17 V. The object can be placed in the nodes by using the tweezers. Note that the levitating object can oscillate horizontally due to air-turbulence; wait a little for things to settle. Small oscillations are not detrimental to measurement results.

- Design, sketch and use a setup to determine as precisely as possible the frequency of the transducers. The speed of sound in air is $v \approx 340 \text{ m/s}$. (2.0 pts)
- Switch *Mode X* to position **I** on the electrical box (F) to change to a different mode of operation where the transducers in the upper half of the levitator are supplied with a *slightly* different frequency ($f + \Delta f$) than the lower one. Describe the changed behaviour of the levitated objects in this mode and determine the frequency difference Δf and its sign. (2.0 pts)

Remember to return the *Mode X* switch to position O for the rest of the exam.

Task E3: Density of solid beads (3.0 pts)

Levitated objects will be situated slightly below the node due to gravity. The restoring acoustic force $\vec{F}$ acting on the levitated object is proportional to P^2 , where $P \propto U$ is the acoustic pressure amplitude at the antinodes and U is the voltage from the power source.

Experimentally determine the density of the unknown beads (O) as precisely as possible. The density of the glass beads (P) is $\rho_{\text{glass}} = 2500 \text{ kg/m}^3$. These spherical beads (O, P) have the same size. (3.0 pts)

Hint: Depending on your approach, for spherical objects and small displacements $\Delta \vec{z}$ from the node, you may use the approximation:

$$\vec{F} = -f(R)P^2\Delta\vec{z} \quad (1)$$

Here, $f(R)$ is some unknown function of the radius R of the levitated object.

Task E4: Evaporation (3.0 pts)

For the remaining tasks, you will levitate liquids, which will form small droplets in the nodes. Place droplets in the levitator using the syringes (R) with needles (S). To avoid cross-contamination, use a separate syringe for each liquid. A good starting voltage for most droplet sizes is 8–12 V; at higher voltages the droplets may explode.

Warning: Avoid spilling liquids on the electronics and the transducers. Keep the metal net (L) on the bottom of the levitator; if it gets wet, remove it and let it dry. If the transducers seem to malfunction, raise your HELP sign.

The exact shape of the levitated droplets can be complicated. Moderately deformed droplets may be approximated as an ellipsoid with semi-axes a, b, c , which has the volume:

$$V = \frac{4\pi}{3}abc \quad (2)$$

In this task, you will study the evaporation of a liquid droplet in the levitator. A simplified description for the evaporation of a droplet with equivalent diameter $D \gtrsim 1.5 \text{ mm}$ is given by:

$$\frac{d(D^2)}{dt} = -\gamma \quad (3)$$

where D is the equivalent diameter of the droplet, i.e., the diameter of a sphere with the same volume V as the real droplet, and γ is the evaporation constant.

For this task, consider only liquid I and keep the voltage constant.

a) Determine the evaporation constant γ in units m^2/s for droplets with an equivalent diameter $D \gtrsim 1.5 \text{ mm}$. (2.5 pts)

b) Would you over- or underestimate the time it takes for a droplet to evaporate entirely, using your result from a)? (0.5 pts)

Task E5: Surface tension (2.5 pts)

The shape of the droplet depends only on its volume V and the ratio P^2/σ . Here, σ is the surface tension of the liquid.

a) Perform a measurement to find out which liquid, I or II, has a lower surface tension. (0.5 pts)

b) Experimentally determine the surface tension of liquid I, given that the surface tension of liquid II is 0.073 N/m . (2.0 pts)

Task E6: Explosion (4.0 pts)

When the acoustic pressure is too high, the levitating droplet will explode. A theoretical formula for the maximum voltage that can be applied to the droplet before it explodes is:

$$U_{\text{max}} = \sqrt{\frac{\alpha}{D} + \beta} \quad (4)$$

where α and β are some constants.

Consider only liquid II for this task.

- a) Determine the constants α and β in the units $\text{V}^2 \cdot \text{mm}$ and V^2 , respectively. (2.0 pts)
- b) Estimate the maximum diameter of a droplet that can be levitated. (2.0 pts)

Task E7: Mysterious line (2.5 pts)

When the levitating droplet becomes rather flat, a levitator voltage can be found for which the light from the red LED passing through the droplet forms a sharp horizontal line on the screen behind.

Consider only liquid III for this task.

Draw a sketch of the ray propagation inside the droplet when the line appears. Use the line phenomenon described above to estimate the refractive index n of liquid III. (2.5 pts)

Hint: For the line to be visible, the LED must be well aligned with the droplet, see Fig. 2.

Task E8: Intentional damage penalty (-0.5 pts)

All equipment and packaging is left on the table after the competition in working condition. For breaking components or packaging due to careless handling or failing to follow the warning in red text, a penalty will be applied. (-0.5 pts)

Equipment

- A. Two green Light Emitting Diodes (LEDs). Do not connect the LEDs to the power supply (G).
- B. Individual transducer.
- C. Metal frame with a levitator module and a red LED, which can be modeled as a *point source*.
- D. Capture unit for collecting falling objects.
- E. 2 hex keys for mounting and aligning the setup.
- F. Electrical enclosure with switches *LED* and *Mode X*.
- G. Power supply.
- H. Banana cables.
- I. Screen.
- J. Tape.
- K. Transparent ruler.
- L. Metal net.
- M. Tweezers.
- N. 15 blue styrofoam beads.
- O. Multiple white spherical beads of unknown material ($\varnothing$ 2.0 mm).
- P. Multiple transparent spherical glass beads ($\varnothing$ 2.0 mm, $\rho_{\text{glass}} = 2500 \text{ kg m}^{-3}$).
- Q. 3 different unknown liquids labelled I, II and III. They are all safe to touch with your hands, but should not be ingested.
- R. 3 syringes.
- S. 3 blunt end needles for the syringes (be careful!).
- T. 2 clothes pegs.
- U. Stop watch.

- V. Lamp.
- W. Power cord.
- X. Piece of paper to dry the metal net (not in image).

If you suspect that a component has failed for some reason during the competition, inform the invigilator to get help.

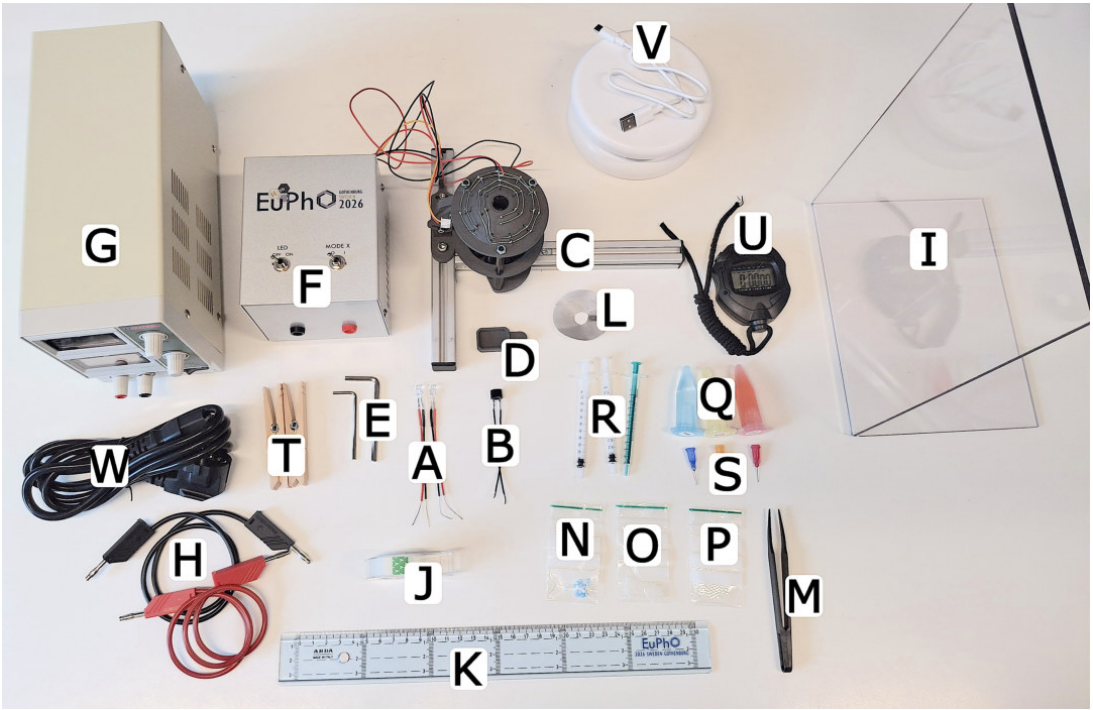


Figure 1: Overview of the equipment.

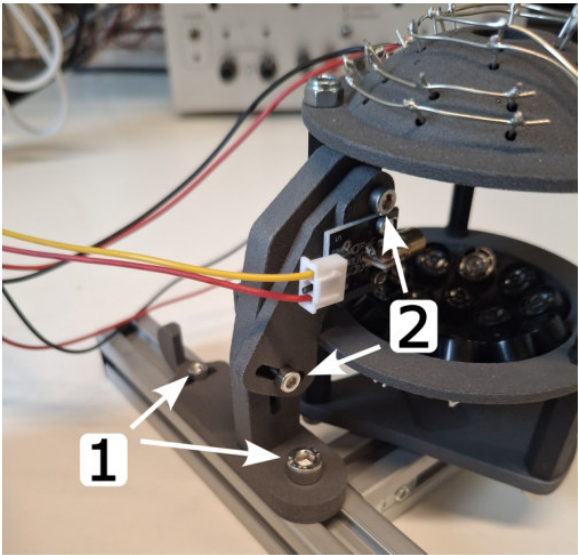


Figure 2: Alignment of LED module. You can align the setup by using the screws shown in the figure. Arrows labelled **1** are for horizontal movement and tilting of the LED module, and arrows labelled **2** are for vertical movement and tilting of the LED module.